

Functional Programming: Exercise 1

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2010 Formosan Summer School
on Logic, Language, and Computation
June 28 – July 9, 2010

Homework due 9:30 am, July 05, 2007.
You must hand in the complete listing of your code.

Note: You need not feel compelled to complete all the problems. Do as many as you can.

Problem 1

Given the following data type definition `'v formula` for formulas of propositional logic (abstracted over a type variable `'v` of propositional letters), define a function `pl` to gather all unique propositional letters in a formula to a list (whose type is `'v list`).

```
type 'v formula =  
  | PL of 'v  
  | Bot  
  | Con of 'v formula * 'v formula  
  | Dis of 'v formula * 'v formula  
  | Imp of 'v formula * 'v formula
```

You may want to first define a function `merge` that takes two lists and return as a result the list of all unique elements appearing in the two input lists. For your reference, the types of `pl` and `merge` are the following:

```
val merge : 'a list -> 'a list -> 'a list = <fun>  
val pl : 'a formula -> 'a list = <fun>
```

Hint: You can use functions `fold_left` and `mem` in O'Caml's `List` module.

Problem 2

Given the following module type definition `BOOLEAN_ALGEBRA`:

```

module type BOOLEAN_ALGEBRA =
sig
  type b
  val cup : b * b -> b
  val cap : b * b -> b
  val inv : b -> b
  val zero : b
  val one : b
end

```

Complete the following parametric module `Evaluator`:

```

module Evaluator (BB : BOOLEAN_ALGEBRA) =
struct
  let rec eval phi v = -----
  let satisfies phi v = (eval phi v) = BB.one
end

```

Note that function `eval` takes as input a formula `phi` and an environment `v` (which maps propositional letters to values of type `BB.b`) and returns as the result the value of `phi` under environment `v`. You can assume that environment `v` is always well-defined.

For your reference, O'Caml shall infer module `Evaluator` to have the following module type:

```

module Evaluator :
functor (BB : BOOLEAN_ALGEBRA) ->
sig
  val eval : 'a formula -> ('a -> BB.b) -> BB.b
  val satisfies : 'a formula -> ('a -> BB.b) -> bool
end

```

Hint: You may want to try out your definition of `Evaluator` on the following module `TruthValues`:

```

module TruthValues : (BOOLEAN_ALGEBRA with type b = bool) =
struct
  type b = bool
  let cup (x, y) = x || y
  let cap (x, y) = x && y
  let inv x = not x
  let zero = false
  let one = true
end

```

```

module TruthValueEvaluator = Evaluator(TruthValues)

```